

**Problem 3 (20 points):** A repair unit working at a local Delta hangar is currently charged with the repair of 5 airplanes  $A_1, \dots, A_5$ . The estimated repair times, in days, for each of these airplanes are 5, 7, 4, 3 and 4. Furthermore, the cost of idle time for each of these airplanes, in \$10,000 per day, are 20, 15, 30, 25 and 20. Assuming that the considered repair unit can work on only one airplane at a time, determine a schedule for working on these airplanes that will minimize the total "idleness" cost incurred for the company.

Let  $C_i$  denote the completing time of the ~~the~~ repair of the  $i$ -th airplane. Then, the incurred <sup>total</sup> "idleness" cost will be  $\sum_{i=1}^5 w_i C_i$ , where  $w_i$  is the daily cost of idleness for these airplanes.

Then, as we explained in class, this cost will be minimized by scheduling the airplanes according to the "weighted SPT" rule, i.e., in increasing sequence of the ratios  $t_i/w_i$ . Hence, the corresponding schedule can be computed as follows

Airplane	1	2	3	4	5
$t_i$	5	7	4	3	4
$w_i$	20	15	30	25	20
$t_i/w_i$	0.25	0.467	0.133	0.12	0.2

So, the optimal schedule is: 4, 3, 5, 1, 2