| Name: |               |
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## ISYE 3027 Test 1

[30] 1. Define sample space, event, and give the three axioms of probability.

2. Suppose P(A) = .3, P(B) = .1, and  $P(B \cap A) = .03$ . What are

- (a)  $P(A^c)$ ?
- (b)  $P(A \mid B)$ ?
- (c)  $P(A \cup B)$ ?
- (d) Are A and B independent?
- (e) Are A and B disjoint?
- 3. Suppose you are dealt 7 cards at random from a standard 52 card deck. In the following questions, do not simplify your answer. Leave it in terms of factorials or ().
  - (a) What is the probability of a flush, i.e., all seven cards coming from one suit?
  - (b) What is the probability of 2 triples, e.g. 3 queens, 3 aces and a king?
- 4. Factory A supplies 3/4 of the components we use, and Factory B supplies the rest. Four percent of Factory A's components and sixteen percent of B's are defective.
  - (a) What proportion of components are defective?
  - (b) Given that a component is defective, what is the probability that it came from Factory A?
- 5. Let  $X_1$  and  $X_2$  be the numbers obtained in two independent throws of a die. Determine  $\Pr\{X_1 + X_2 > 6 \mid X_1 > X_2\}$ ?
- 6. Bonus: Whose matchboxes?

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